

# Mathematical Model of a Three-Phase Induction Motor with Asymmetrical Twelve-Zone Stator Windings

Valerii Tytyuk  
Department "Artificial Intelligence  
Technologies"  
JSC "Karaganda Industrial  
University"  
Temirtau, Kazakhstan  
v.tytyuk@ttu.edu.kz

Tatyana Sivetskaya  
Department "Power Engineering"  
JSC "Karaganda Industrial  
University"  
Temirtau, Kazakhstan  
t.sivetskaya@ttu.edu.kz

Oleksii Chornyi  
Institute of Electromechanics, Energy  
Saving and Automatic Control Systems  
Kremenchuk Mykhailo Ostrohradskii  
National University  
Kremenchuk, Ukraine  
alekseii.chornyi@gmail.com

Mila Baranovskaya  
Department of Electromechanics  
Kyiv Riih National University  
Kyiv Riih, Ukraine  
baranovska@knu.edu.ua

Victor Bousher  
Dept. of Electrical Engineering and  
Electronics  
National University "Odessa Maritime  
Academy"  
Odessa, Ukraine  
victor.v.bousher@gmail.com

Vitalii Kuznetsov  
Department of the electrical  
engineering  
Ukrainian State University of Science  
and Technologies  
Dnipro, Ukraine  
wit1975@i.ua

**Abstract**—The paper proposes a mathematical model of a three-phase induction motor with an asymmetrical twelve-zone winding of stator with parallel connection of subwindings. The mathematical model was developed using the theory of generalized electromechanical converter and contains equations of electrical equilibrium of six stator windings and three rotor windings. The equations for calculating the electromagnetic moment and the equations of motion of the induction motor with an asymmetrical twelve-zone stator winding rotor were obtained. The developed mathematical model in the form of cell-matrix equations has been implemented in MATLAB/Simulink.

**Keywords**—induction motor, asymmetrical twelve-zone winding, generalized

electromechanical converter, mathematical modelling.

## I. INTRODUCTION

It is known that induction motors (IM) and electric drives based on them are one of the most significant consumers of electrical energy in the structure of world energy consumption. This is due to the wide scope of these engines in modern industrial production. The known standard IEC 60034 [1] obliges manufacturers to search for new ways to minimize losses in electrical machines.

In world practice, there are two main directions for solving this problem. The first direction is the transition to a controlled electric drive based on semiconductor frequency converters (FC) [2– 6], that makes it possible to supply the end user with the power required at a particular moment [7].

## REFERENCES

- [1] Commission Regulation (EC) No 640/2009: implementing Directive 2005/32/EC of the European Parliament and of the Council with regard to ecodesign requirements for electric motors, PDF, 22 July 2009
- [2] H. Sarhan, Energy Efficient Control of Three-Phase Induction Motor Drive. *Energy and Power Engineering*, vol. 3, pp. 107-112, 2011. doi:10.4236/epe.2011.32014.
- [3] C. Thanga Raj, S. P. Srivastava, and Pramod Agarwal, "Energy Efficient Control of Three-Phase Induction Motor - A Review," *International Journal of Computer and Electrical Engineering* vol. 1, no. 1, pp. 61-70, 2009.
- [4] M. A. Magzoub, N. B. Saad, R. B. Ibrahim, Efficiency Improvement of Induction Motor Variable Speed Drive Using a Hybrid Fuzzy-fuzzy Controller, *Energy Procedia*, vol. 75, pp. 1529-1535, 2015, ISSN 1876-6102, <http://dx.doi.org/10.1016/j.egypro.2015.07.309>.
- [5] Zagirnyak, M., Maliakova, M. & Kalinov, A. "Analysis of electric circuits with semiconductor converters with the use of a small parameter method in frequency domain," *COMPEL – The International Journal for Computation and Mathematics in Electrical and Electronic Engineering*, vol. 34, no. 3, pp. 808-823. (2015)
- [6] V. Melnykov, A. Kalinov, "Compensation the induction motor parametrical asymmetry", *Technical Electrodynamics*, no. 3, pp. 85-86, 2012
- [7] M. Zagirnyak, A. Kalinov, M. Maliakova, "An algorithm for electric circuits calculation based on instantaneous power component balance", *Przegląd Elektrotechniczny*, vol. 87, no. 12 B, pp. 212-215, 2011.
- [8] F. J. T. E. Ferreira, A. T. de Almeida. Novel Multiflux Level, Three-Phase, Squirrel-Cage Induction Motor for Efficiency and Power Factor Maximization. *IEEE Transactions on Energy Conversion*, vol. 23, no. 1, pp. 101-109, March 2008. doi: 10.1109/TEC.2007.914355
- [9] Levi E., Bojoi R., Profumo F., Toliyat H.A., Williamson S., Multiphase induction motor drives - a technology status review, *IET Electr. Power Appl.*, pp. 489-516, 2007.
- [10] I. González-Prieto, M. J. Duran, and F. J. Barrero, "Fault-tolerant control of six-phase induction motor drives with variable current injection," *IEEE Trans. Power Electron.*, vol. 32, no. 10, pp. 7894–7903, Oct. 2017.
- [11] F. Barrero and M. J. Duran, "Recent advances in the design, modeling and control of multiphase machines—Part 1," *IEEE Trans. Ind. Electron.*, vol. 63, no. 1, pp. 449–458, Jan. 2016.
- [12] A. R. Munoz and T. A. Lipo, "Dual stator winding induction machine drive," in *IEEE Transactions on Industry Applications*, vol. 36, no. 5, pp. 1369-1379, Sept.-Oct. 2000, doi: 10.1109/28.871286.
- [13] B. Kundrotas, S. Lisauskas, and R. Rinkeviciene, "Model of Multiphase Induction Motor", *ELEKTRON ELEKTROTECH*, vol. 111, no. 5, pp. 111-114, Jun. 2011.
- [14] V. Tytiuk, Y. Modlo, A. Berdai, S. Kikovka, V. Busher and Z. Rozhnenko, "Exploring the MMF of a Three-Phase Induction Motor with Twelve-Zone Stator Windings," 2021 IEEE International Conference on Modern Electrical and Energy Systems (MEES), 2021, pp. 1-4, doi: 10.1109/MEES52427.2021.9598786.
- [15] S.Kikovka, V.Tytiuk, O.Ilchenko, "Exploring the Operational Characteristics of a Three-Phase Induction Motor with Multi-Zone Stator Windings," *Proceedings of the 2017 IEEE International Conference on Modern electrical and energy systems (MEES)*, 2017. –pp. 120-124.
- [16] V.Tytiuk, O.Ilchenko, O.Chorny, I.Zachepa, S.Serhiienko, & A. Berdai, (2019). SRM identification with fractional order transfer functions. In 2019 IEEE 2nd Ukraine Conference on Electrical and Computer Engineering (UKRCON) (pp. 271-274). IEEE.
- [17] Tryputen, M., Kuznetsov, V., Kuznetsova, A., Tryputen, M., Kuznetsova, Y., Serdiuk, T. Improving the Reliability of Simulating the Operation of an Induction Motor in Solving the Technical and Economic Problem (2021) *Advances in Intelligent Systems and Computing*, 1247 AISC, pp. 143-152. DOI: 10.1007/978-3-030-55506-1\_13